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Second Semester M.Tech. Degree Examination, December 2011
Modern Control Engineering

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Derive the equation of motion of a simple spring mass and damper system and devote the characteristic equation. (10 Marks)
- b. The transfer of a system is $\frac{8}{s^2 + 4s + 8}$
 Find :
 i) Natural frequency
 ii) Damping ratio
 iii) Damped natural frequency
 iv) Peak time and peak overshoot. (10 Marks)
- 2 Sketch the root locus for : $G(s)H(s) = \frac{K(s+4)}{s(s^2 + 2s + 2)}$ and ascertain the nature of stability. (20 Marks)
- 3 a. For a unity feedback system $G(s) = \frac{10}{s(s+1)(s+4)}$ obtain analytically, the gain margin and phase margin. (10 Marks)
- b. Define : i) Gain Margin (G.M) ; ii) Phase Margin (PM). (06 Marks)
- c. Define the any four advantages of Bode plots. (04 Marks)
- 4 a. Explain M and N circle. (08 Marks)
- b. Using Nyquist stability criterion, find the range of k for closed – loop stability
 $G(s)H(s) = \frac{K(4s+1)}{s(s-1)}$. (12 Marks)
- 5 a. Define state – space method. Solve the following, using direct programming.
 $y(t) = \frac{D+3}{(D+1)(D+2)} f(t)$ (10 Marks)
- b. For a system represented by $\dot{X} = AX$, the response is
 $x(t) = \begin{bmatrix} 2e^{-4t} \\ e^{-4t} \end{bmatrix}$ when $X(0) = \begin{bmatrix} 2 \\ 1 \end{bmatrix}$ and $\dot{x}(t) = \begin{bmatrix} 4e^{-2t} \\ e^{-2t} \end{bmatrix}$ when $X(0) = \begin{bmatrix} 4 \\ 1 \end{bmatrix}$
 Determine the system matrix A and the state transition matrix. (10 Marks)

- 6 a. Find the Z – transform of the following :
- i) $x(n) = 2^n u(n)$
 - ii) $x(n) = f(n)$
 - iii) $x(n) = n u(n)$ (12 Marks)
- b. Find the inverse Z – transform of $x(z)$, using the partial fraction expansion approach
- $$x(z) = \frac{z+1}{3z^2 - 4z + 1} \quad (08 \text{ Marks})$$
- 7 a. Explain with a neat sketch, computer controlled system. Obtain its controller characteristics. (10 Marks)
- b. The transfer function for a plant is $\frac{(s+2)}{[s(s+1)]}$. Determine the characteristics of a digital controller, such that, the response of the system to a unit step function will be $c(t) = 5(1 - e^{-2t})$. The sampling period is $T = 1.0s$. (10 Marks)
- 8 a. Define node and branch, as applied to a signal flow graph.
- b. Distinguish between steady state and transient response.
- c. Explain state variable concepts.
- d. Define the characteristic equation. (20 Marks)
